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US Army Corps of Engineers

The Hydrologic Engineering Center



GENERALIZED COMPUTER PROGRAM

MULTIPLE LINEAR REGRESSION



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September 1970



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MULTIPLE LINEAR REGRESSION

THE HYDROLOGIC ENGINEERING CENTER GENERALIZED COMPUTER PROGRAM 704-G1-L2020

INTRODUCTION

1. ORIGIN OF PROGRAM

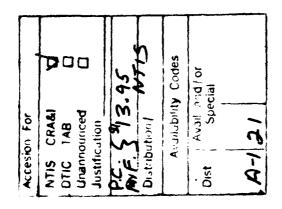
This program was developed in The Hydrologic Engineering Center by R. G. Willey and H. E. Kubik. A two-part FORTRAN II version was written in 1968; a September 1970 version was written in FORTRAN IV and included increased capability, and this version basically modifies the input to conform with present standards.

It is recognized that nearly all computer centers have access to multiple linear regression programs, but this program includes some different statistical philosophy and some capability that is particularly useful for regional analyses.

2. CAPABILITIES OF PROGRAM

The program makes a multiple linear regression analysis and has the following special features:

- a. <u>Automatic deletion</u>. The analysis is first made with all of the specified independent variables and then the least significant variable is deleted and the analysis repeated.
- b. Variable selection. All independent and dependent variables can be stored and then only those variables desired for a particular analysis may be used.
- c. Combination of variables. New variables may be computed from the input variables, e.g., a parameter $A\sqrt{S}$ [basin area(A) times the square root of main channel slope (S)] can be computed when area and slope have been input.
- d. <u>Transformations</u>. The variables may be transformed (square root, logarithmic or reciprocal) to more nearly linearize the relations.





e. <u>Input regression parameters</u>. The regression constant and regression coefficients may be input and the residuals (difference between observed and calculated), the adjusted multiple determination coefficient and the standard error of estimate will be computed.

3. HARDWARE AND SOFTWARE REQUIREMENTS

This program has been developed and tested primarily on the UNIVAC 1108 and the CDC 7600 computer. No tape units are required.

PROGRAM DESCRIPTION

4. PROGRAM ORGANIZATION

The program consists of a main program and two subroutines. Subroutine COMB is used to compute a new variable based on a combination of one or more variables. Subroutine CROUT solves a set of simultaneous equations to obtain the regression coefficients. The program will exit normally only in the main program. A macro-flow chart of the program organization is shown in figure 1.

THEORETICAL ASSUMPTION AND LIMITATIONS

The computations are made in accordance with the procedures given in "Statistical Methods in Hydrology" by Leo R. Beard, January 1962. The independent variables are deleted, in turn, based on the minimum adjusted partial determination coefficient (\overline{r}^2) .

The adjusted multiple determination coefficient is used to compute the standard error of estimate. Care must be taken in insuring that there are more observations than variables. If the number of observations are very close to the number of variables, the results may be unreasonable.

Variables with zero or very little (.000001) variance are deleted from the analysis. A diagnostic is printed stating the name of the variable deleted because of this limitation.

6. METHODS OF COMPUTATION

The regression analysis is performed on either the transformed or non-transformed variables in a like manner. The basic equation is:

$$Y = a + \sum_{i=1}^{n} b_i X_i$$
 (1)

where the X_i values are the independent variables and the Y value is the dependent variable. "n" is the number of independent variables in the analysis. The regression coefficients (b_i) are calculated using the Crout Method (Exhibit 1) for solution of the following equations:

$$\Sigma(x_{1})^{2} b_{1} + \Sigma(x_{1}x_{2}) b_{2} + \cdots + \Sigma(x_{1}x_{n}) b_{n} = \Sigma(yx_{1})$$

$$\Sigma(x_{1}x_{2}) b_{1} + \Sigma(x_{2})^{2} b_{2} + \cdots + \Sigma(x_{2}x_{n}) b_{n} = \Sigma(yx_{2})$$

$$\vdots \qquad \vdots \qquad \vdots \qquad \vdots$$

$$\Sigma(x_{1}x_{n}) b_{1} + \Sigma(x_{2}x_{n}) b_{2} + \cdots + \Sigma(x_{n})^{2} b_{n} = \Sigma(yx_{n})$$

$$(2)$$

where x_i is the deviation of the value X for variable i, the observation number being implied, from the mean (\overline{X}_i) . $\Sigma(x_i)^2$ and $\Sigma(x_ix_j)$ can be determined from the following equations:

$$\Xi(x_{i})^{2} = \Xi(x_{i} - \overline{x}_{i})^{2} = \Xi(x_{i})^{2} - (\Sigma x_{i})^{2}/N$$
 (3)

$$\mathbb{T}(\mathbf{x}_{i}\mathbf{x}_{i}) = \mathbb{T}(\mathbf{X}_{i} - \overline{\mathbf{X}}_{i})(\mathbf{X}_{i} - \overline{\mathbf{X}}_{i}) = \mathbb{T}(\mathbf{X}_{i}\mathbf{X}_{i}) - \mathbb{T}\mathbf{X}_{i} \mathbb{T}\mathbf{X}_{i}/N \tag{4}$$

where N is the number of events or observations.

The regression constant (a) is calculated by use of the equation:

$$a = \overline{Y} - \frac{n}{i} b_i \overline{X}_i$$
 (5)

where \overline{Y} is the mean of the dependent variable for N events and the \overline{X} , values are the means of each of the independent variables for N events.

The unadjusted (R^2) and the adjusted (\overline{R}^2) determination coefficients are determined by the following equations:

$$R^{2} = \frac{b_{1} \pi(yx_{1}) + b_{2} \pi(yx_{2}) + \dots + b_{n} \pi(yx_{n})}{\pi(y)^{2}}$$
(6)

$$\overline{R}^2 = 1 - (1 - R^2)(N - 1)/(N - NVAR)$$
 (7)

where NVAR is total number of variables (both dependent and independent) in the analysis.

The partial determination coefficient for a variable is the percent increase in unexplained variance caused by deleting that variable from the regression equation. The adjusted partial determination coefficient is calculated by the following equation:

$$\overline{r}^{2}14.23 = \frac{(1-\overline{R}^{2}_{1.23}) - (1-\overline{R}^{2}_{1.234})}{1-\overline{R}^{2}_{1.23}}$$
(8)

where the first subscript for the adjusted partial determination coefficient indicates the dependent variable, the second indicates the independent variable whose partial determination coefficient is being computed, and the subscripts after the decimal indicate the other independent variables involved in the computation.

The standard error of estimate (S_p) is calculated by the following equation:

$$S_e = \sqrt{(1-\overline{R}^2)\pi(y)^2/(N-1)} = S_y \sqrt{1-\overline{R}^2}$$
 (9)

where $S_{\mathbf{y}}$ is the standard deviation of the dependent variable.

When the residual prediction option is specified the "RESIDUAL" column is calculated as the difference between the observed and predicted values. The "ERROR AS DEVIATE" column is calculated as the residual divided by the standard deviation. The "RATIO" column is calculated as the residual divided by the observed value.

EXHIBIT 1

Crout's Mothod*

One of the best methods for solving systems of linear equations on desk calculating machines was developed by P. D. Crout in 1941. This method is based on the elimination method, with the calculations arranged in systematic order so as to facilitate their accomplishment on a desk calculator. In this method the coefficients and constant terms of the equations are written in the form of a "matrix," which is a rectangular array of quantities arranged in rows and columns.

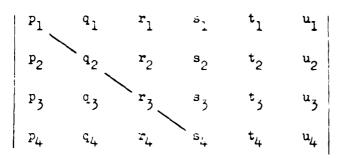
The method is best explained by an example. Suppose that in a multiple correlation analysis it is required to solve the following system of linear equations to obtain the unknown values of b_2 , b_3 , b_4 and b_n .

For simplicity let us replace the coefficients of the b's by the letters p, q, r and s, and the constant terms by the letter t, using subscripts 1, 2, 3 and 4 to denote the respective equations:

$$p_1 \ b_2 + q_1 \ b_3 + r_1 \ b_4 + s_1 \ b_5 = t_1$$
 $p_2 \ b_2 + q_2 \ b_3 + r_2 \ b_4 + s_2 \ b_5 = t_2$
 $p_3 \ b_2 + q_3 \ b_3 + r_3 \ b_4 + s_3 \ b_5 = t_3$
 $p_4 \ b_2 + q_4 \ b_3 + r_4 \ b_4 + s_4 \ b_5 = t_4$

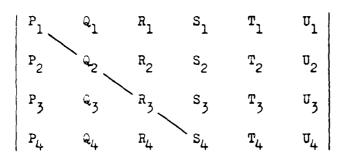
A continuous check on the computations as they progress may be obtained by adding to the matrix of the above system a column of u's, such that u = p + q + r + s + t. The matrix and check column are written as follows:

The Crout Method was presented at the AIEE Summer Convention in June 1941 by Prescott D. Crout. The method was developed by Gauss and refined by Doolittle.



The elements p_1 , q_2 , r_3 and s_4 form the "principal diagonal" of the matrix. Examination of the original equations shows that the coefficients are symmetrical about the principal diagonal, i.e., $q_1 = p_2$, $r_1 = p_3$, $r_2 = q_3$, $s_1 = p_4$, $s_2 = c_4$, and $s_3 = r_4$. This is characteristic of the system of equations to be solved in any multiple correlation analysis. Because of this symmetry, the computations are considerably simplified. While the Crout method may be used to solve any system of linear equations, the computational steps given here are applicable only to those with symmetrical coefficients.

The solution consists of two parts, viz., the computation of a "derived matrix" and the "back solution." Let the derived matrix be denoted as follows:



The elements of the derived matrix are computed as follows:

The general pattern of the above computations, which may be applied to a system containing any number of equations, is as follows:

- (1) The first column of the derived matrix is copied from the first column of the given matrix.
- (2) The remaining elements in the first row of the derived matrix are computed by dividing the corresponding elements in the first row of the given matrix by the first element in that row.
- (3) After completing the $n\frac{th}{t}$ row, the remaining elements in the $(n+1)\frac{th}{t}$ column are computed. Such an element (X) equals the corresponding element of the given matrix minus the product of the element immediately to the left of (X) by the element immediately above the principal diagonal in the same column as (X), minus the product of the second element to the left of (X) by the second element above the principal diagonal in the same column as (X), etc. After each element below the principal diagonal is recorded, and while that element is still in the calculator, it is divided by the element of the principal diagonal which is in the same column. The quotient is the element whose location is symmetrical to (X) with respect to the principal diagonal.

(4) When the elements in the $(n+1)\frac{th}{t}$ column and their symmetrical counterparts have been recorded, the $(n+1)\frac{th}{t}$ row will be complete except for the last two elements, which are next computed. Such an element (X) equals the corresponding element of the given matrix minus the product of the element immediately above (X) by the element immediately to the left of the principal diagonal in the same row as (X), minus the product of the second element above (X) by the second element to the left of the principal diagonal in the same row as (X), etc., all divided by the element of the principal diagonal in the same row as (X).

The check column (U) of the derived matrix serves as a continuous check on the computations in that each element in the column equals one plus the sum of the elements in the same row to the right of the principal diagonal. That is,

This check should be made after completing each row.

The elements of the derived matrix to the right of the principal diagonal form a system of equations which may now be used to compute the unknown values of b₂, b₃, b₄ and b₅ by successive substitution.

This is known as the "back solution." The computations are as follows:

$$b_5 = T_4$$
 $b_4 = T_3 - S_3 b_5$
 $b_3 = T_2 - S_2 b_5 - R_2 b_4$
 $b_2 = T_1 - S_1 b_5 - R_1 b_4 - Q_1 b_3$

It is very important that the computations be carried to a sufficient number of digits, both in computing the coefficients and constant terms of the original equations, and in computing the elements of the derived matrix. It is possible for relatively small errors in the coefficients and constant terms of the original equations to result in relatively large errors in the computed solutions of the unknowns. The

greatest source of error in computing the elements of the derived matrix arises from the loss of leading significant digits by subtraction. This must be guarded against and can be done by carrying the computations to more figures than the data. As a general rule, it is recommended that the coefficients and constant terms of the original equations be carried to a sufficient number of decimals to produce at least five significant digits in the smallest quantity, and that the elements of the derived matrix be carried to one more decimal than this, but to not less than six significant digits.

```
T1
T2
T3
J1
                          JANUARY 1975
          TEST NO. 1
   STATISTICAL METHODS (BEARD 1962) EX 33
        FIRST ANALYSIS-DATA SUPPLIED
NM
          LOG Q LOG SNO LOG GWLOG PRCP 1 1 1 1
TR
                                                                            2
             . 939
DT
     1935
                        . 393
                                 .325
                                           .710
              . 945
     1937
OT
                        .343
                                 . 385
                                           .534
     1938
             1.052
TY
                        . 369
                                 .408
                                           . 886
              . 744
                        . 246
                                 .428
TC
     1939
                                           .581
                        .181
Σī
     1940
              .566
                                 . 316
                                          1.027
                        . 297
. 299
     1941
TC
             1.081
                                 .460
                                          1.315
     1942
                                 .511
DT
             1.960
                                          1.097
                        . 354
                                 .379
                                          .707
יוַרָ
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                        . 295
بلد
             1.021
                                 . 395
     1344
                                          1.240
              .920
                                 . 376
יזעו
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                        .321
                                          1.091
              . 755
                        .168
                                  .413
יוכו
     1945
                                          1.038
יות
     1947
                        .280
               .960
                                           .979
                                  . 410
ED
NI,T
        DATA FROM PREVIOUS ANALYSIS
T3
ÜR
        30011
NJ
         TEST NO.2 JANUARY 1979
DATA WITH SPECIAL FORMAT
T1
                          JANUARY 1975
Т3
         COMPUTATION OF NEW VARIABLE
   AREA LENGTH (A2, A5, 3F8.0/8X,F8.0)
MM
                                SLOPE
                                          LOG Q
C. I
                  1 L/S**.5
      9
<u>cc</u>
       -3
                                     5
                                               6
                                                       -2
                                                                  1
                                                                           7
                                                                                     4
TR
        4 3 0 0 1 3
DT
   IDP R
               230
                        38.8
                                 1.27
   IDP R
             3.082
DГ
DT BUF
        007
             19.4
                        10.9
                                15.42
DI MCD C
              7.52
                         7.0
                                 9.56
             2.062
DTSALT
             32.5
2.568
        1
                        10.9
                                13.04
DTSALT
DTSALT
               114
        2
                        36.8
                                 3.01
        2
DTSALT
             3.004
DT 2DP R
DT 2DP R
             635
3.557
                        88.1
                                 1.06
ED
ED
NJ
         TEST NO. 3
4
                         JANUARY 1975
Т2
         USE DATA FROM TEST NO. 1
T3
         READ REGRESSION COEFFICIENTS
J1
          LOG Q LOG SNO LOG GWLOG PRCP
NM.
TR
                                                                          - 1
    -.22
RP
              ,939
    1936
                        .399
                                 . 325
                                           .710
DT
     1937
DI
              .945
                        . 343
                                 . 385
                                           .634
     1938
             1.052
                        . 353
                                 .408
                                           . 886
Dr
             .744
                                           .591
                        . 246
OT
    1939
                                 .428
              .555
T
     1940
                        .181
                                 .316
                                          1.027
                        . 297
DT
     1941
             1.081
                                 .460
                                          1.315
                                 .511
                        . 299
     1942
             1.050
                                          1.097
DT
                        .354
    1943
              .892
                                 .379
                                           .707
Dr
     1944
                                 395
                                          1.240
DT.
             1.021
DT
     1945
             .920
                        .321
                                 . 376
                                          1.091
              . 755
                        . 168
     1345
                                 .413
or
                                          1.038
     1947
              .960
                        . 280
                                          .979
DI
                                 .410
ED
NJ
```

TEST DATA CUTPUT

MULTIPLE LINEAR REGRESSION

704-G1~L2020 JAN 1975 REVISED JAN 1933

TEST NO. 1 JANUARY 1975 STATISTICAL METHODS (BEARD 1962) EX 33 FIRST ANALYSIS-DATA SUPPLIED

NVAL NOOMB IPRNT IFRMT DELE DELTA
4 0 0 0 0 0.0000

+ + + + + ANALYSIS NO 1 + + + +

DEPENDENT VARIABLE -- LOG O

VARIABLE TRANSFORMATION
LOG Q NONE
LOG SNO NONE
LOG GW NONE
LOG PRCP MONE

INPUT DATA

OBS NO OBS ID LOG Q LOG SNO LOG GW LOG PRCP 1 1936 0.939 0.399 0.325 0.710 2 1937 0.945 0.343 0.385 0.534 0.369 1938 1.052 0.408 0.886 3 4 1939 0.744 0.246 0.428 0.581 5 0.656 0.131 1.027 1940 0.316 0.297 5 1941 1.091 0.4501.315 0.2997 1942 1.050 0.511 1.097 Я 1).354 1943 0.8320.3799.707 3 1944 1.021 n. 295 0.395 1.240 1945 10 0.920 0.321 0.376 1.091 11 1946 0.755 0.168 0.413 1.038 12 1347 0.960 0.280 0.410 0.979

STATISTICS OF DATA

BASED ON 12 OBSERVATIONS

			STANDARD	
VARTABLE	AVERAGE	VARIANCE	DEVIATION	
LOG SNO	0.3960	0.0050	0.0704	
LOG GW	0.4005	0.0028	0.0531	
LOG PROP	0.9421	0.0572	0.2392	
roc 5	0.9196	0.0181	0.1346	DEPENDENT VARIABLE

SIMPLE CORRELATION COEFFICIENTS

VARTABLE	LOG SNO	LOG GW	LOG PRCP	LOG Q
LOG SNO	1.0000	0.0000	-0.0459	0.6308
LOG GW	0.0000	1.0000	0.1275	0.4170
LOG PRCP	-0.0459	0.1275	1.0000	0.2011
rue 5	0.5308	0.4170	0.2011	1.0000

INDEPENDENT	REGRESSION	PART	TAL
VARIABLE	COEFFICIENT	DETERMI COEFFI	
LOG SNO	1.621805	0.9	106
LOG GW	1.012931	0.6814	
LOG PRCP	0.273387	0.74	151
			STANDARD
REGRESSION	R	R BAR	ERROR OF
CONSTANT	SQUARE	SQUARE	ESTIMATE
-0.223704	0.9437	0.9226	0.0374

+++++

VARIABLE DELETED IS LOG GW

	EPENDENT VARIABLE	REGRE COEFFI	ession Icient	PART: DETERMII COEFFI	NATION	
	LOG SNO	1 6	547213	0.74	5.7	
	OG PROP		348730	0.59		
200	, pp. 2.10.1			0.020	STANDARD	
	RESSION NSTANT	R SQUAF	or .	r bar Square	ERROR OF ESTIMATE	
	0.103475	აჯე გ ი მ.801		0.7570	0.0663	
			1	0.7370	0.5563	
DEPENDE	ENT VARIAE	BLE LOG Q			ERROR AS	
000 110	one ra	anaenuen avi	י מינו א מוסט	RESIDUAL	DEVIATE	RATIO
OBS NO 1	1936	OBSERVED CAI	1.008	-0.059	-0.515	-0.074
2	1937	0.945	0.990	0.055	0.412	0.059
	1938	1.052	1.020	0.03?	0.236	0.030
4	1939	0.744	0.711	0.033	0.243	0.044
5	1940	0.666	J.760	-0.094	-0.697	-0.141
6	1941	1.081	1.051	0.030	0.221	0.027
7	1942	1.060	0.979	0.091	0.605	0.077
8	1943	0.892	0.933	-0.041	-0.306	-0.046
3	1944	1.021	1.022	-0.901	-0.006	-0.001
10	1945	0.920	1.013	-0.093	-0.689	-0.101
11	1946	0.755	υ.742	0.013	0.095	0.017
12	1947	0.960	0.906	0.954	0.400	0.056
		R BAR SOU	ARED	0.7570		
	STANDARD !	ERROR OF ESTI		0.0563		
•		MEAN E		0.0000		
	M	EAN SQUARED E		0.0033		

Page 4 of 11

VARIABLE DELETED IS LOG PRCP

IND	EPENDENT	RE	GRESSION	PART	TAL	
V.	ARIABLE	COE	FFICIENT	DETERMINATION		
				COEFFICIENT		
	LOG SNO		1.286212	0.39	79	
					STANDARD	
DEC.	RESSION	,	R	R BAR	ERROR OF	
	NSTANT			SQUARE		
	.538865	0.4		0.3979	0.1044	
U	רניפטנר.	0.4	DZ9	0.3979	0.1044	
DEPENDE	NT VARIA	BLE LOG	0			
					ERROR AS	
OBS NO	OBS ID	OBSERVED (CALCULATED	RESIDUAL	DEVIATE	RATIO
1	1936	0.939	1.052	-0.113	-0.840	-0.120
2	1937	0.945	0.980	-0.035	-0.260	-0.037
3	1938	1.052	1.013	0.039	0.286	0.937
1	1939	0.744	0.855	-0.111	-0.827	-0.150
5	1940	0.566	0.772	-0.106	-0.785	-0.159
6	1941	1.081	0.921	0.160	1.190	0.148
7	1942	1.060	0.923	0.137	1.015	ე.129
8	1943	0.892	0.994	-0.102	-0.759	-0.115
9	1944	1.021	0.918	0.103	0.763	0.101
10	1945	3.920	0.952	-0.032	-0.236	-0.034
11	1946	0. 7 55	0.755	0.000	0.000	0.000
12	1947	0.960	0.899	0.061	0.453	0.064
		R BAR S	-	0.3979		
S	TANDARD I	ERROR OF ES	TIMATE	0.1044		
		MEAN	ERROR	0.0000		
	MI	ean squared	ERROR	0.0091		

MULTIPLE LINEAR REGRESSION

704-G1-L2020 JNV 1975 REVISED JAI 1983

TEST NO. 1 JANUARY 1975 STATISTICAL METHODS (BEARD 1962) EX 33 DATA FROM PREVIOUS ANALYSIS

+ + + + ANALYSIS NO 2 + + + +

DEPENDENT VARIABLE -- LOG GW

IDEP	TRANSFORMATION CODES	NOBR	IRES	IFORC
3	0 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0	o	0	n

VARIABLE	TRANSE DRMATION
ruc 5	MOL ARED
LOG SNO	VOT USED
LOG GW	NONE
LOG PRCP	NONE

INPUT DATA

OBS	MO	OBS ID	LOG GW	roc ppcp
055	4O	082 10	אים פונוגן	LOG PRCP
	1	1936	0.325	0.710
	2	1937	0.385	0.534
	3	1938	0.408	0.886
	4	1939	0.428	0.581
	5	1940	0.316	1.027
	6	1941	0.460	1.315
	7	1942	0.511	1.097
	9	1943	0.379	0.707
	9	1944	0.395	1.240
	10	1945	0.376	1.091
	11	1946	0.413	1.038
	12	1947	0.410	0.979

STATISTICS OF DATA

BASED ON 12 OBSERVATIONS

VARTABLE	AVERAGE	VARIANCE	STANDARD DEVIATION	
LOG PROP	0.9421	0.0572	0.2392	
LOG GW	0.4005	0.0028	0.0531	DEPENDENT VARIABLE

SIMPLE CORRELATION COEFFICIENTS

VARTABLE	LOG PRCP	LOG GW
LOG PRCP	1.0000	0.1275
LOG GW	0.1275	1.0000

INDEPENDENT VARIABLE	REGRESSION COEFFICIENT	PART DETERMI COEFFI	INATION
LOG PRCP	0.072132	0.0	163
			STANDARD
REGRESSION	R	R BAR	ERROR OF
CONSTANT	SQUARE	SQUARE	ESTIMATE
0.332546	0.1057	0.0163	0.0526

MULTIPLE LINEAR REGRESSION

704-G1-L2020 JAN 1975 REVISED JAN 1983

TEST NO.2 JANUARY 1975
DATA WITH SPECIAL FORMAT
COMPUTATION OF NEW VARIABLE

NVAL NCOMB IPRNT IFRMT IDELE DELTA
4 1 0 1 0 0.0000

DATA FORMAT (A2, A5, 3F8.0/9X, F8.0)

COMBINATION 1 STEP 1 2 3 4 5 6 7 8 9 OPERATION CODE -3 1 8 5 6 -2 1 7 4 CONSTANTS 1/ 0.5000

+ + + + + ANALYSIS NO 1 + + + +

DEPENDENT VARIABLE -- LOG Q

VARIABLE TRANSFORMATION
AREA COMMON LOG
LENGTH NOT USED
SLOPE NOT USED
LOG Q NONE
L/S**.5 COMMON LOG

INPUT DATA

AREA OBS NO OBS ID LOG Q L/S**.5 IDP R 230.000 3.082 34.429 1 BUF C 2 19.400 2.377 2.776 3 MCD C 7.520 2.052 2.252 4 SALT 1 32.500 2.568 3.018 21.211 85.570 5 SALT 2 114.000 3.004 635.000 3.557 6 2DP R

STATISTICS OF DATA

BASED ON	-	OD CROUX B LONG
D15 5 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	• • •	OBSERVATIONS

73R143D°	A. tork st.	CARCANCE	STANDARD DEVIATION	
rathe. M	1.316.	U. 5165	0.7189	
L/s**.5	1.0119	0.4526	0.5727	
rog 5	2.7750	0.2936	0.5413	DEPENDENT VARIABLE

SIMPLE CORRELATION COEFFICIENTS

VARTABLE	AREA	L/S**.5	rog ð
AREA	1.0000	0.9658	0.9936
6/9**.5	0.9658	1.0000	0.9566
rog S	0.9936	0.9566	1.0000

INDEPENDENT	REGRESSION	PAR	TIAL
VARIABLE	COEFFICIENT	DETERM	INATION
		COEFFI	CLENT
AREA	0.780995	0.90	004
L/S**.5	-0.934300	0.00	000
			STANDARD
REGRESSION	R	R BAR	ERROR OF
CONSTANT	SQUARE	SQUARE	ESTIMATE
1,391251	0.9898	0.9830	0.0705

VARIABLE DELETED IS L/S**.5

INATION	PART DETERMI COEFFI	REGRESSION COEFFICIENT	INDEPENDENT VARIABLE
372	0.99	0.749774	AREA
STANDARD			
ERROR OF	R BAR	Ř	REGRESSION
ESTIMATE	SQUARE	SQUARE	CONSTANT
0.0614	0.9872	0.9397	1.413246

MULTIPLE LINEAR REGRESSION

704-G1-L2020 JAN 1975 REVISED JAN 1983

REVISED JAN 1983

TEST NO. 3 JANUARY 1975 USE DATA FROM TEST NO. 1 READ REGRESSION COEFFICIENTS

NVAL NCOMB IPRNT IFRMT IDELE DELTA 4 0 1 0 0.0000

+ + + + ANALYSIS NO 1 + + + +

DEPENDENT VARIABLE -- LOG Q

VARIABLE TRANSFORMATION
LOG Q NONE
LOG SNO NONE
LOG GW NONE
LOG PRCP NONE

STATISTICS OF DATA

BASED ON 12 OBSERVATIONS

			STANDARD	
VARIABLE	AVERAGE	VARIANCE	DEVIATION	
LOG SNO	0.2960	0.0050	0.0704	
LOG GW	0.4005	0.0028	0.0531	
LOG PRCP	0.9421	0.0572	0.2392	
LOG O	0.9196	0.0181	0.1346	DEPENDENT VARIABLE

SIMPLE CORRELATION COEFFICIENTS

VARIABLE	LOG SNO	LOG GW	LOG PRCP	rog ó
LOG SNO	1.0000	0.0000	-0.0459	0.6309
LOG GW	0.0000	1.0000	0.1275	0.4170
LOG PRCP	-0.0459	0.1275	1.0000	0.2011
rue õ	0 6308	0 4170	0 2011	1 0000

INPUT REGRESSION COEFFICIENTS

CONSTANT -0.2200

LOG SNO	1.6000
LOG GW	1.0000
LOG PRCP	0.3000

DEPENDENT	TARTARTE.	LOG O

					ERROR AS	
OBS NO	OBS ID	OBSERVED	CALCULATED	RESIDUAL	DEVIATE	RATIO
1	1936	0.939	v.956	-0.017	-0.129	-0.019
2	1937	0.945	0.904	0.041	0.305	0.043
3	1938	1.052	1.044	ე.008	0.058	0.007
4	1939	0.744	J.776	-0.032	-0.237	-0.043
5	1940	0.555	0.694	-0.028	-0.206	-0.042
6	1941	1.091	1.110	-0.029	-0.213	-0.027
7	1942	1.060	1.098	-0.038	-0.286	-0.036
8	1943	0.892	0.937	-0.045	-0.338	-0.051
9	1944	1.021	1.019	0.002	0.015	0.002
10	1945	0.920	0.997	-0.077	-0.571	-0.084
11	1946	0 .7 55	0.773	-0.018	-0.135	-0.024
12	1947	0.960	0.932	0.028	0.210	0.029

r bar squared	0.9190
STANDARD ERROR OF ESTIMATE	0.0383
MEAN ERROR	-0.0171
MEAN SOHARED ERROR	0.0013

DESCRIPTION OF INPUT DATA GENERALIZED COMPUTER PROGRAM 704-G1-L2020

T1, T2, T3 Title Cards

Three title cards for the identification of the ouput. A T1 must be in columns 1 and 2 of the first card. A new T3 card is required for each subsequent analysis which uses the same data set.

J1 - First Job Card

Field (1)	Variable	Value	<u>Description</u>
Ι.	NVAL		Total number of values (variables) to be read for each observation and stored for use in this and subsequent analyses. This is not necessarily the number of variables to be included in the first analysis which will be specified by the TR card. Dimensioned for 18 variables.
2.	NCOMB		Number of new variables to be computed by combining two or more variables and constants. All combinations for subsequent analyses which use the same data must be performed in first analysis. Dimensioned for five combinations. Sum of NVAL and NCOMB must not exceed 18.
3.	IPRNT		Data list options.
		0	Provides list of input data for each job.
		1	Suppresses listing of input data.

⁽¹⁾ The standard card format for most HEC programs consists of columns 1 2 reserved for the card code (Field 0) and the remaining columns used for program specification or data. Columns 3-8 are Field 1 and the remaining 72 columns are divided into nine 8-column fields.

J1 Card (continued)

Field	Variable	Valué	Description
4.	I FRMT		Format of data on the cards.
		0	Data in standard format of (A2,A6,9F8.0) for card identification, observation identification, and data, respectively. The format for the second card, if required, is (8X,9F8.0).
		1	Special format will be read on FT card.
5.	IDELE		Deletion options.
		Û	Automatic deletion of each variable with lowest partial determination coefficient, in turn, until only one independent variable remains.
		ī	Suppresses automatic deletion.
6-10.			Not used.

NM - Variable Name Card

Field	Variab e	Value	Description
1.	DELTA		Increment which will be added to <u>all</u> data to meet certain constraints when logarithmic, square root, or reciprocal transformations are made. The increment should be zero unless the following constraints are violated:
			Transform Constraint Logarithmic "data" + DELTA >0 Square root "data" + DELTA >0 Reciprocal "data" + DELTA <0
2-10.	ANAMA		Alphanumeric name of each variable read in, NVAL (Jl.1) names. Order must correspond to order of data as read. If more than one card is needed, the name for the loth variable is placed in field 2 of the second card, etc.

FT - Special Format Card

Supply this card only if IFRMT (J1.4) is positive.

<u>Field</u>	<u>Variable</u>	<u>Value</u>	Description
1-10.	IFMT		Format of data to be read from cards. The first field must read the data card code (the DT) in A2 format and the second field must provide for an alphanumeric identification of the observation in A format and NVAL (Jl.1) floating point fields, e.g., (A2, A4, 10X, 10F6.0). The second A field cannot exceed six columns. NOTE: Parentheses must be provided in specification.

CJ - Combination Job Card (1)

Field	Variable	Value	Description
1.	NOP		Number of operation codes necessary to compute a new variable by combining one or more variables. Dimensioned for 20 operation codes.
2.	NCØN		Number of constants necessary to compute a new variable. Dimensioned for five constants.
3.	ANAMA		Alphanumeric name of new variable being computed.
4-10.			Not used.

\underline{C} - Combination Operations Card (1)

Supply this card only in conjunction with CJ card.

<u>Field</u>	Variable	Value	Description
1-10.	IOP		Operation to be performed, NOP (CJ.1) values.

⁽¹⁾ Provide NCOMB (J1.2) sets of CJ, CO, and, if required, CC cards.

CO Card (continued)

The sequence of operations necessary to obtain a desired computed variable must be specified by "operation codes." These operations are performed by using three operating registers, argument (ARG), accumulator (ACC) and storage (STORE). The accumulator has been initialized to zero prior to computations. Any constants necessary for the arithmetic will be entered on the CC card in the sequence necessary. The final value in the accumulator is used as the value for the new variable.

Operation		Operation Code
Variable→ARG	-vn	Variable number, preceded by minus sign, to use next where "vn" is order number as read in or combined. This variable becomes the argument.
ARG+ACCACC	1	Add argument to accumulator.
ACC-ARG→ACC	2	Subtract argument from accumulator.
ARG(ACC)-+ACC	3	Multiply argument times accumulator.
ACC/ARG→ACC	4	Divide accumulator by argument.
ACC ^{ARG} →ACC	5	Raise accumulator to power of argument.
ACC→STGRE then O.→ACC	6	Store accumulator while further arithmetic is done. Accumulator is then reset to zero.
STCRE→ARG	7	Retrieve stored value. This value now becomes the argument.
Corstant→ARG	8	Use the next constant on the CC card as the argument.

CC - Combination Constants Card (1)

Supply this card only if NCON (CJ.2) is positive.

Field	Variable	Value	Description
1-5.	CNST		Supply NCON (CJ.2) values.
6-10.			Not used.

⁽¹⁾ Provide NCOMB (J1.2) sets of CJ, CO, and, if required, CC cards.

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TR - Analysis Specification Card

This card is provided for each analysis.

Field	Variable	<u>Value</u>	Description
1.	IDEP		Number identifying the order number of the dependent variable in the total array of values read in, i.e., 3 if third value in the array is the desired dependent variable.
2-6.	IFUNC		Variable deletion or transformation code for each variable. NVAL (Jl.1) plus NCOMB (Jl.2) values in special (I2) format, i.e., the code for the first variable read would be in column 10, the code for the second variable in column 12, etc.
			Operation
		0	Delete from current analysis
		1	No transformation
		2	Square root
		3	Logarithmic, base 10
		4	Reciprocal
7.	NUBR		The number of observations to be used in this analysis. The program will count the number of observations (NOBS) as the data are read; therefore, may be left blank if all observations are to be used in analysis. If positive, the first NOBR observations will be used, but must be less than or equal to NOBS. Dimensioned for 500 observations.
8.	IRES		Residual-prediction options. Provides a tabulation of the observed, calculated, the difference between the observed and calculated, and, if the log transformation of the dependent variable, the ratio of the observed to the calculated. The computation for a multiple linear regression analysis will be performed when IRES 20. Predetermined regression parameters will be read (RP card) when IRES -1.

TR Card (continued)

Field	Variable	Value	Description
		-1	Regression parameters to be read in with \underline{no} analyses.
		0	Suppresses residualprediction routine.
		>0	Positive number indicating maximum number of independent variables to be included in equation. Routine will operate for each deletion thereafter.
9-10.			Not used.

RP - Regression Parameters Card

Supply this card only if IRES (TR.8) is -1.

Field	Variable	Value	Description
1.	AA		Regression constant.
2.	ВВ		Regression coefficients. Supply same number of coefficients as there are independent variables (one less than the number of IFUNC (TR.2) values that are greater than zero) in the order corresponding to data.

DT - Input Data Cards

Input data need only be provided for first analysis. Subsequent analyses can use same data provided all necessary data are read in first analysis. The data may be in the following format or the format specified by the FT card. Dimensioned for 500 observations.

<u>Field</u>	<u>Variable</u>	<u>Value</u>	Description
1.	XID		An alphanumeric identification for the observation.
2.	X		Value for the first variable.

DT Card (continued)

<u>Field</u>	<u>Variable</u>	Value	Description
3~10.	X		Value for succeeding variables, NVAL (Jl.1) values. If more than one card is needed, the value for the 10th variable is placed in field 2 of the second card, etc. The identification (XID) can be repeated in field 1 to assist in identifying each card.

ED - End of Data Card

Supply the same number of ED cards as required to supply one observation on DT cards.

Field	Variable	<u>Value</u>	Description
0.	ID		The letters ED $\underline{\text{must}}$ appear in columns 1 and 2.
1-10.			Not used.

NJ - Next Job Card

Field	Variable	Value	Description
1.	NEXT		This variable indicates what type of job follows according to the following values:
		0	Begin a new job. Branches to beginning of program and reads T1, T2, and T3 cards for a new job or for a normal stop.
		1	Different analysis with same input data. Branches to read T3, TR, and, if required, RP cards. (No data cards provided.)

Il card, plus three blank cards, will cause a normal STOP.

